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# Decision fusion with corrupted reports in multi-sensor networks

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## **Summary**

- Introduction and motivation
- Distributed detection in adversarial setting
- Asymptotic Information-theoretic analysis
- Decision fusion with byzantine nodes
  - Optimum decision fusion: a game-theoretic approach
  - A simplified approach based on message passing
- Conclusions and directions for future research



#### **Distributed detection setup**

$$\mathbf{x}_i = (x_{i,1}, x_{i,2} \dots x_{i,m})$$

Observation vector available to i-th node

$$\mathbf{u}_i = (u_{i,1}, u_{i,2} \dots u_{i,m})$$

Report sent to FC by i-th node



- FC performs a *Binary Hypothesis Test* on system state.
- The test often aims at detecting when the system exits a safe state S<sub>0</sub>



#### A wide variety of applications

- Wireless sensor networks
- Spectrum sensing for cognitive radio
- Intrusion detection
- Network monitoring
- Anomaly detection
- Smart grid
- Social networks
- Reputation systems
- Multi-clue decision making



#### **Distributed detection in adversarial setting**

- An attacker may corrupt part of the system to induce a decision error
- Different versions:
  - Corrupted observations
  - **Corrupted nodes**
  - **Corrupted reports**





# Asymptotic Information-theoretic analysis



#### **Basic assumptions**

- System state does not change over time
- Number of observations for each node goes to infinity  $(m \rightarrow \infty)$
- Game-theoretic approach
- Similarity with SI game [1], solution provided in [2]

[1] M.Barni, B.Tondi, The Source Identification Game: an Information-Theoretic Perspective, IEEE Trans. on Information Forensics and Security, vol. 8, no. 3, pp. 450 –463, March 2013.

[2] M. Barni, B. Tondi, "Multiple-Observation Hypothesis Testing under Adversarial Conditions", Proc. of WIFS 2013, IEEE Int. Workshop on Information Forensics and Security, Ghuanzhou, China, 18-21 November 2013, pp. 91-96.



## **Game Theory in a nutshell**

#### Two-player game

$$\begin{split} G(S_1,S_2,u_1,u_2) \\ S_1 &= \left\{ s_{1,1},s_{1,2}\ldots s_{1,n1} \right\} & \text{Set of strategies available to first player} \\ S_2 &= \left\{ s_{2,1},s_{2,2}\ldots s_{n2} \right\} & \text{Set of strategies available to second player} \\ u_1(s_{1,i},s_{2,j}) & \text{Payoff of first player for a given profile} \\ u_2(s_{1,i},s_{2,j}) & \text{Payoff of second player for a given profile} \end{split}$$

## Competitive (zero-sum) game

 $\mathbf{u}_1(\cdot,\cdot)=-\mathbf{u}_2(\cdot,\cdot)$ 

#### Sequential vs strategic vs multiple moves games



# Equilibrium

#### **Optimal choices**

In game theory we are interested in the optimal choices of rational players

## (stricly) Dominant strategy

The best strategy regardless of the other player's move

$$u_1(s_1^*, s_2) > u_1(s_1, s_2) \quad \forall s_1 \in S_1 \quad \forall s_2 \in S_2$$

... then equilibrium is

$$(s_1^*, s_2^*)$$
 with  $s_2^*$  such that  
 $u_2(s_1^*, s_2^*) \ge u_2(s_1^*, s_2) \quad \forall s_2 \in S_2$ 



## Equilibrium

## Nash equilibrium

No player gets an advantage by changing his strategy assuming the other does not change his own

$$u_1(s_1^*, s_2^*) \ge u_1(s_1, s_2^*)$$
 ∀ $s_1 ∈ S_1$   
 $u_2(s_1^*, s_2^*) \ge u_2(s_1^*, s_2)$  ∀ $s_2 ∈ S_2$ 

#### ... and many others

- worst case assumption
- rationalizable equilibrium

<sup>- ...</sup> 

#### The SI game (with multiple observations)

#### Payoff and structure of the game: *Neyman-Pearson*

- D aims at minimizing the false negative error probability  $P_{fn}$  under the constraint that  $P_{fp}$  stays below a threshold.
- Omniscient A. He/she acts only under S1, his aim being the maximization of  $\mathsf{P}_{\mathsf{fn}}$
- > Zero-sum game:  $u_A = -u_D = P_{fn}$

#### **Space of D's strategies**

- All detection regions based on *on first order (possibly joint) statistics*;
- Asymptotic version of the problem: constraint on asymptotic decay rate of  $P_{fp}$  ( $P_{fp} < 2^{-\lambda m}$ )

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#### Several versions of the game

 D has full knowledge of system statistics and bases the decision on all the available information still relying on first order statistics





 D still has full knowledge of system statistics but observes only the marginals

 D has full knowledge of system statistics but decides by fusing local decisions



#### Some noticeable results proven in [2]

- The game theoretic formulation of the problem is dominance solvable
- Optimum fusion strategy checks if the joint empirical pmf of the observations is in accordance with the expected one. For the full statistics case we have

$$\Lambda_0^* = \left\{ \hat{P} \in \mathcal{P}_m : \mathcal{D}(\hat{P}||P_{\mathbf{x}}) < \lambda - |\mathcal{X}|^k \frac{\log(m+1)}{m} \right\}$$

- The optimum fusion strategy does NOT pass from the identification of malevolent nodes
- Under certain assumptions, reliable decision is possible even in the presence of only one uncorrupted node

[2] M. Barni, B. Tondi, "Multiple-Observation Hypothesis Testing under Adversarial Conditions", Proc. of WIFS 2013, IEEE Int. Workshop on Information Forensics and Security, Ghuanzhou, China, 18-21 November 2013, pp. 91-96.

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# Decision fusion with Byzantines

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#### **Decision fusion with Byzantines**



- Now system state changes over time
- The fusion center makes its choice based on the results of the local decisions made at the nodes
- Global decision on *m* states
- Corrupted nodes

   (called Byzantines [3])
   may submit wrong
   reports

[3] A. Vempaty, L. Tong, P. Varshney, "Distributed Inference with Byzantine Data", Signal Processing Magazine, vol. 30, no. 5, September 2013



#### **Possible approaches**

- Byzantines isolation
  - A. S. Rawat, P. Anand, H. Chen, and P. K. Varshney, "Collaborative spectrum sensing in the presence of Byzantine attacks in cognitive radio networks," IEEE Trans. Signal Process., vol. 59, no. 2, pp. 774–786, Feb. 2011.
  - A. Abrardo, M. Barni, K. Kallas, and B. Tondi, "Decision fusion with corrupted reports in multi-sensor networks: A game-theoretic approach," in Proc. IEEE Conf. Decision Control (CDC), Los Angeles, CA, USA, Dec. 2014, pp. 505– 510.

#### Byzantine-tolerant schemes

 M. Gagrani, P. Sharma, S. Iyengar, V. Nadendla, A. Vempaty, H. Chen, and P. Varshney, "On noise-enhanced distributed inference in the presence of Byzan-tines," in Proc. 49th Annu. Allerton Conf. Communications Control Comput-ing, Sept. 2011, pp. 1222–1229.

#### Optimum fusion



#### System and attack model

• Equiprobable independent system states

 $P_{S_i}(0) = P_{S_i}(1) = 0.5$ 

- Constant and independent local decisions errors
- Symmetric local decision errors

 $\varepsilon = \Pr(U_{i,j} \neq S_j)$ 

• Byzantines flip local decision with probability P<sub>mal</sub>

 $Pr(U_{i,j} \neq R_{i,j} \mid \text{node is Byzantine}) = P_{mal}$ 

- Byzantines flip decisions independently of each other (non cooperative malicious nodes) and on subsequent states
- Nodes status and Byzantines' strategy do not change over time



#### **Optimum fusion rule**

If all the parameters of the system are known the optimum decision rule at the FC can be derived as follows

 $s^m$  = sequence of system

 $a^n$  = vector with states of

states

nodes

$$s^{m,*} = \arg \max_{s^m} P(\overline{s^m} | \overline{\mathbf{r}}) \quad \text{MAP estimate}$$

$$s^{m,*} = \arg \max_{s^m} P(\mathbf{r} | s^m) \quad \text{ML estimate}$$

$$s^{m,*} = \arg \max_{s^m} \sum_{a^n} P(\mathbf{r} | a^n, s^m) P(a^n)$$

$$= \arg \max_{s^m} \sum_{a^n} \left( \prod_{i=1}^n P(\mathbf{r}_i | a_i, s^m) \right) P(a^n)$$

$$= \arg \max_{s^m} \sum_{a^n} \left( \prod_{i=1}^n \prod_{j=1}^m P(r_{ij} | a_i, s_j) \right) P(a^n)$$



#### **Optimum fusion rule**

 $\delta = \varepsilon (1 - P_{mal}) + (1 - \varepsilon) P_{mal}$  Prob that FC receives a wrong report

 $m_{eq}(i)$  Number of times for which the report of node *i* is equal to the state

$$s^{m,*} = \arg \max_{s^m} \sum_{a^n} \left( \prod_{i:a_i=0} (1-\varepsilon)^{m_{eq}(i)} \varepsilon^{m-m_{eq}(i)} \right) \prod_{i:a_i=1} (1-\delta)^{m_{eq}(i)} \delta^{m-m_{eq}(i)} P(a^n)$$

To go on it is necessary to make some assumptions on the distribution of byzantine nodes across the network:  $P(a^n)$ 



#### **Byzantines distribution**

#### 1. Unconstrained maximum entropy distribution

Letting  $P_{mal} = 1$  forces the mutual information between *S* and *R* to zero making any meaningful decision impossible

2. Constrained maximum entropy distribution, fixed E[N<sub>B</sub>] Entropy is maximized by assuming i.i.d. node states with

$$\alpha = Pr(A_i = 1) = E[N_B]$$

$$\arg\max_{s^m} \prod_{i=1}^n \left[ (1-\alpha)(1-\varepsilon)^{m_{eq}(i)} \varepsilon^{m-m_{eq}(i)} + \alpha(1-\delta)^{m_{eq}(i)} \delta^{m-m_{eq}(i)} \right]$$

The complexity of the optimum fusion rule is linear in n and exponential in m



#### **Byzantines distribution**

3. Constrained maximum entropy distribution,  $N_B < n/2$ 

Equiprobable  $a^n$  (only those for which  $N_B < n/2$ )

# Complexity of optimum fusion rule is exponential in *m* and quadratic in *n* (dynamic programming [3])

[4] A. Abrardo, M. Barni, K. Kallas, B. Tondi, "A Game-Theoretic Framework for Optimum Decision Fusion in the Presence of Byzantines", *IEEE Trans. Information Forensics and Security*, vol.11, no. 6, 2016

$$s^{m,*} = \arg \max_{s^m} \sum_{I \in \mathcal{I}_{n_B}} \left( \prod_{i \in I} (1-\delta)^{m_{eq}(i)} \delta^{m-m_{eq}(i)} \right)$$
$$\prod_{i \in \mathcal{I} \setminus I} (1-\varepsilon)^{m_{eq}(i)} \varepsilon^{m-m_{eq}(i)} \right)$$



## A game theoretic perspective

- Application of the optimum fusion rule requires that the FC knows  $\ensuremath{\mathsf{P}_{\mathsf{mal}}}$
- Large values of P<sub>mal</sub> are more effective in inducing a decision error
- If byzantine nodes are identified  $P_{mal} = 1$  does not make any harm
- With  $P_{mal} = 0.5$  we have I(S,R) = 0
- Which value of P<sub>mal</sub> should the Byzantines choose?
- How can the FC know the vale of  $P_{mal}$ ?
- We adopt a game-theoretic perspective



## **Decision fusion with Byzantines game**

Two-player game (Byzantines collectively playing as a single player)

 $\mathcal{S}_B = \{P_{mal}^B \in [0, 1]\}$  $\mathcal{S}_{FC} = \{P_{mal}^{FC} \in [0, 1]\}$ 

Payoff equal to error probability at the fusion center

Strategic game



• Run simulations by quantizing the set of strategies

 $P_{mal} = \{0.5, 0.6, 0.7, 0.8, 0.9, 1.0\}$ 

- Length of observation window *m* plays a major role
- We run simulations with small and medium values of *m*
- Show results for n = 20,  $\varepsilon = 0.1$

$$-m = 4$$

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- *m* = 10



#### Small *m*, independent node states

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	0.33	0.37	0.44	0.58	0.73	0.85
0.6	0.60	0.54	0.59	0.70	0.80	1.14
0.7	1.38	1.20	1.19	1.24	1.29	2.40
0.8	3.88	3.56	3.36	3.31	3.35	6.03
0.9	9.93	9.61	9.57	9.55	9.54	11.96
1.0	20.33	20.98	21.70	21.90	21.84	(19.19)

 $P_{e} x 10^{2}$ 

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	0.62	0.69	0.86	1.34	1.70	1.57
0.6	1.23	1.15	1.26	1.84	2.18	2.38
0.7	2.94	2.64	2.57	3.00	3.14	5.33
0.8	7.89	7.39	7.03	6.74	6.81	12.73
0.9	18.45	17.94	17.63	17.08	17.07	22.78
1.0	34.39	34.62	34.84	36.66	36.61	(33.14)

$$\alpha$$
 = 0.45, n = 20

P<sub>e</sub> x 10<sup>2</sup>



## Small *m*, fixed number of Byzantines

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	(3.80)	3.80	4.60	7.60	12.0	29.0
0.6	3.60	3.45	3.90	5.20	8.0	17.0
0.7	3.45	2.80	2.80	3.10	4.40	8.75
0.8	4.10	2.85	2.15	2.05	2.25	3.25
0.9	3.55	2.05	1.40	0.95	0.70	0.75
1.0	2.05	0.90	0.35	0.15	0.05	0.05

$$N_B = 6, n = 20$$
  
m = 4

P<sub>e</sub> x 10<sup>4</sup>

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	0.22	0.24	0.33	0.63	1.41	4.13
0.6	0.27	0.24	0.27	0.41	0.78	2.03
0.7	0.32	0.24	0.23	0.26	0.37	0.82
0.8	0.54	0.45	0.39	0.36	0.41	0.59
0.9	2.04	1.87	1.76	1.58	1.56	1.66
1.0	9.48	8.76	8.37	6.72	5.88	5.51

$$N_{\rm B} = 9, n = 20$$

$$P_{e} \ge 10^{2}$$



## Small *m*, fixed number of Byzantines

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	1.2	1.4	1.9	3.1	6.3	18.9
0.6	1.5	1.4	1.4	2.0	3.7	10.0
0.7	1.4	1.1	0.945	1.1	1.7	4.0
0.8	1.4	0.95	0.715	0.58	0.675	1.2
0.9	2.1	1.4	0.995	0.745	0.71	0.78
1.0	7.3	5.7	5.3	3.7	3.0	2.9

$$N_B = 8, n = 20$$
  
m = 4  
 $P_e \ge 10^4$ 

#### Nash equilibrium exists only in mixed strategies

	0.5	0.6	0.7	0.8	0.9	1.0
$P(P^B_{mal})$	0.179	0	0	0	0	0.821
$P(P_{mal}^{FC})$	0	0	0	0.844	0.156	0
		$P_e^* =$	= <b>3.</b> 8e	- 4		



#### Medium *m*, independent node states

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	0.11	0.13	0.19	0.73	2.16	0.68
0.6	0.11	8.32e-2	9.96e-2	0.26	0.67	1.30
0.7	0.18	7.66e-2	6.62e-2	9.52e-2	0.18	4.87
0.8	1.10	0.60	0.33	0.24	0.28	10.41
0.9	5.77	4.75	3.95	3.53	3.41	13.44
1.0	20.41	21.26	22.65	24.27	26.21	18.72

$$\alpha = 0.4, n = 20$$
  
m = 10

$$P_{a} \times 10^{2}$$

			-		-	
$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	0.20	0.23	0.47	2.88	10.92	1.26
0.6	0.22	0.18	0.24	0.80	2.85	2.93
0.7	0.50	0.19	0.15	0.23	0.65	10.64
0.8	2.61	1.24	0.63	0.41	0.59	20.65
0.9	11.74	9.28	7.08	5.65	5.21	25.85
1.0	34.25	34.94	36.01	37.74	39.87	(33.17)

$$\alpha$$
 = 0.45, n = 20



#### Medium *m*, fixed number of Byzantines

$P^B_{mal}/P^{FC}_{mal}$	0.5	0.6	0.7	0.8	0.9	1.0
0.5	(1.22)	1.22	1.40	2.20	5.06	11.0
0.6	1.12	0.94	1.02	1.26	2.56	5.34
0.7	1.22	0.58	0.56	0.64	0.98	2.06
0.8	1.22	0.36	0.32	0.28	0.30	0.56
0.9	1.40	0.20	0.18	0.16	0.10	0.18
1.0	1.52	0.14	0.14	0.10	6e-2	4e-2

$$N_B = 6, n = 20$$
  
m = 10  
 $P_e \ge 10^4$ 

For  $N_B = 8$  and  $N_B = 9$ , a Nash equilibrium exists only in mixed strategies

	0.5	0.6	0.7	0.8	0.9	1.0
$P(P^B_{mal})$	0.4995	0	0	0	0	0.5005
$P(P_{mal}^{FC})$	0	0	0.66	0.34	0	0
		$P_e^* = 1$	1.58e -	3		

$$N_B = 9, n = 20$$
  
m = 10



#### Performance at the equilibrium

	Maj	HardIS	SoftIS	OPT
Independent nodes, $\alpha = 0.3$	0.073	0.048	0.041	0.035
Independent nodes, $\alpha = 0.4$	0.239	0.211	0.201	0.192
Independent nodes, $\alpha = 0.45$	0.362	0.344	0.338	0.331
Fixed n. of nodes $n_B = 6$	0.017	0.002	6.2e-4	3.8e-4
Fixed n. of nodes $n_B = 8$	0.125	0.044	0.016	0.004
Fixed n. of nodes $n_B = 9$	0.279	0.186	0.125	0.055
Max entropy with $N_B < n/2$	0.154	0.086	0.052	0.021
Max entropy with $N_B < n/3$	0.0041	5e-4	2.15e-4	1.9e-4

ε = 0.1 n = 20

m = 4

#### [Maj] Majority rule

[HardIS] A. S. Rawat, P. Anand, H. Chen, and P. K. Varshney, "Collaborative spectrum sensing in the presence of Byzantine attacks in cognitive radio networks," IEEE Trans. Signal Process., vol. 59, no. 2, pp. 774–786, Feb. 2011.

[SoftIS] A. Abrardo, M. Barni, K. Kallas, and B. Tondi, "Decision fusion with corrupted reports in multisensor networks: A game-theoretic approach," in Proc. IEEE Conf. Decision Control (CDC), Los Angeles, CA, USA, Dec. 2014, pp. 505–510.



- Complexity prevents the use of optimum decision fusion for large m
- Use of message passing (MP) to develop a fast nearly optimum detector at the FC
- MP is a nearly optimum iterative optimization procedure based computation on graphs theory
- The MP-based algorithm allows to extend our results to cases with large observation windows [5]

[5] A. Abrardo, M. Barni, K. Kallas, B. Tondi, "A Message Passing Approach for Decision Fusion in Adversarial Multi-Sensor Networks", *Information Fusion*, vol. 40, March 2018, pp. 101-111

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## **Results (small m)**



We can now evaluate the performance also when *m* is large and for markovian sources



#### **Results**



For large m the optimum detector can not be applied. The performance of MP-fusion remain very good



#### **Results: optimum attack strategy**



The tendency of passing from  $P_{mal} = 1$  to  $P_{mal} = 0.5$  for large values of m is confirmed (for nearly optimum decision fusion)



#### Synchronized attack

- Using a synchronized attack may increase significantly the effectiveness of the attack
- We assume that the Byzantines share the values assumed by a local source of randomness q = (q<sub>1</sub>, q<sub>2</sub> ... q<sub>m</sub>)
- The optimum fusion rule can be easily derived by incorporating the value assumed by the local randomness into the maximization

$$s_{i}^{*} = \arg \max_{s_{i} \in \{0.1\}} \sum_{\{\mathbf{sqa}\} \setminus s_{i}} \prod_{i,j} p(r_{ij}|s_{i}, q_{i}, a_{j}) \prod_{h} p(s_{h}|s_{h-1}) \prod_{k} p(q_{k}|q_{k-1}) \prod_{l} p(a_{l})$$

Which can be implemented again by exploiting the sum product MP algorithm [6]

[6] A. Abrardo, M. Barni, K. Kallas, B. Tondi, "A Message Passing Approach for Decision Fusion of Hidden-Markov Observations in the presence of Synchronized Attacks", Proc. of MMEDIA17, 9-th Int. Conf. on Advances in Multimedia, April 23-27, 2017, Venice, Italy.



#### **Results**



The synchronized attack is by far more powerful than the asynchronous one. Game-theoretic analysis still on-going.

#### **Conclusions and future research**

- The case studied here is only an oversimplified example
- Many interesting extensions are possible:
  - Time varying attacks
  - Allow communication among Byzantines
  - Non-binary reports
  - Coalition games

- ...

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- Distributed detection
  - K. Kallas, B. Tondi, M. Barni, "Consensus Algorithm with Censored Data for Distributed Detection with Corrupted Measurements: A Game-Theoretic Approach", *Proc. of GameSec* 2016, Conference on Decision and Game Theory for Security, November 2-4, 2016, New York, NY, USA



#### **Conclusions and future research**

- Application to real cases
  - Network monitoring
  - Wireless sensor networks
    - Surveillance
    - Drone detection
    - . . .
  - Social networks
    - Crowdcomputing
- Implementation in testbed



# Thank you for your attention