

*WIFS 2022*

*14-th Int. Workshop Information Forensics and Security*

# ***Adversarial examples: threat or scarecrow***

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# Outline

- The threat
- Just another effect of the curse of dimensionality?
- What's so special with DL?
- Threat or scarecrow
- Looking ahead

# The big-bang: everything started with [1]

[1] C. Szegedy, W. Zaremba, I. Sutskever, J. Bruna, D. Erhan, I. Goodfellow, R. Fergus (2013). Intriguing properties of neural networks. *arXiv preprint arXiv:1312.6199*.



*«We find that deep neural networks learn input-output mappings that are fairly discontinuous to a significant extent. We can cause the network to **misclassify an image by applying a certain hardly perceptible perturbation**, which is found by maximizing the network's prediction error»*

# Since then ...



Classified  
as a *cat*

Highly magnified attack



Classified  
as a *dog*

# Striking examples: one pixel attack

**AllConv**



**SHIP**  
CAR(99.7%)



**HORSE**  
DOG(70.7%)



**CAR**  
AIRPLANE(82.4%)

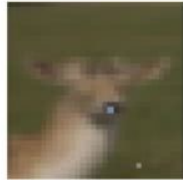
**NiN**



**HORSE**  
FROG(99.9%)



**DOG**  
CAT(75.5%)



**DEER**  
DOG(86.4%)

**VGG**



**DEER**  
AIRPLANE(85.2%)



**BIRD**  
FROG(86.5%)



**CAT**  
BIRD(66.2%)



**DEER**  
AIRPLANE(49.8%)



**HORSE**  
DOG(88.0%)



**BIRD**  
FROG(88.8%)



**SHIP**  
AIRPLANE(62.7%)



**SHIP**  
AIRPLANE(88.2%)



**CAT**  
DOG(78.2%)

# Not only digital



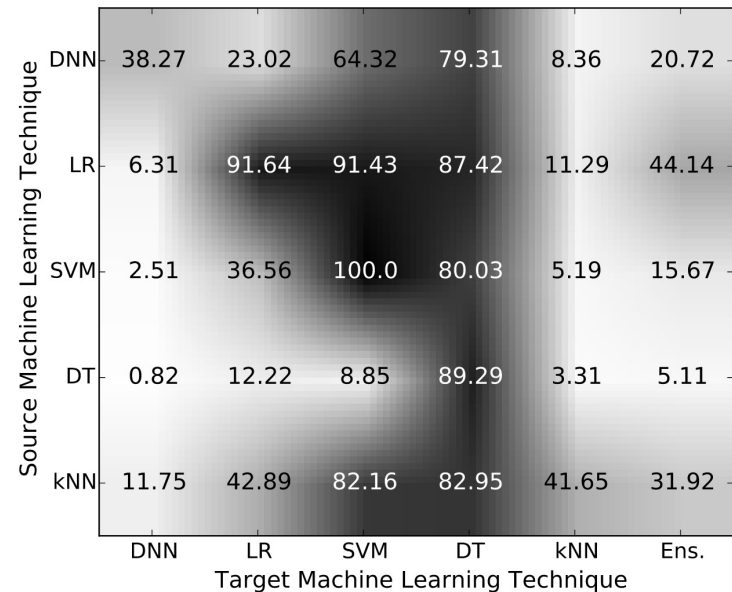
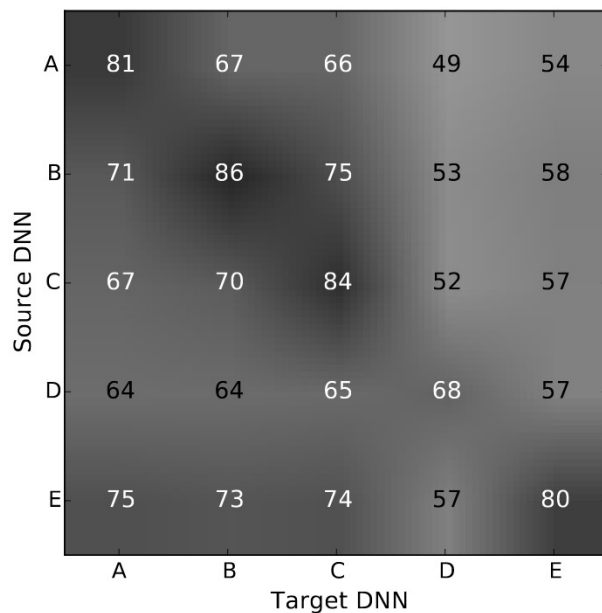
# Not only digital



# Attacks transferability

- Concerns turned into panic when (a certain degree of) transferability of adversarial examples was proven [1]

[1] N. Papernot, P. McDaniel, I. Goodfellow. "Transferability in machine learning: from phenomena to black-box attacks using adversarial samples." *arXiv preprint arXiv:1605.07277* (2016).





# A not-so-recent history

- [1] M. Barreno, B. Nelson, A. D. Joseph, J. D. Tygar, “The security of machine learning”, Mach Learn 81, pp. 121–148, 2010.
- [2] N. Dalvi, P. Domingos, P. Mausam, S. Sanghai, D. Verma, “Adversarial classification”. Proc. ACM SIGKDD, 2004.
- [3] D. Lowd and C. Meek, “Adversarial learning” in Proc. of the ACM SIGKDD Conf. 641-647, 2005.
- [4] B. Biggio, et al. "Evasion attacks against machine learning at test time." Joint European conf. machine learning and knowledge discovery in databases. Springer, Berlin, Heidelberg, 2013.
- [5] B. Biggio, F. Roli, (2018). Wild patterns: Ten years after the rise of adversarial machine learning. Pattern Recognition, (84).

... and previous similar results in watermarking, biometrics, adversarial multimedia forensics ...

# A not-so-recent history

- Yet the alarm raised only with the rise of deep learning
- Why? What's special with deep learning?
  - Popularity and importance of Deep Learning
  - Not only

# Setting

Focus on

- White box (perfect knowledge) attacks
- (Binary) classification networks
- Non-targeted attacks
  - Extension to targeted attacks is non-trivial
  - No distinction in the binary case
- Goal: answer the question:  
*Is there a special relationship between DL and the existence of adversarial examples?*

# The linear explanation\*

$$f(x) = \text{Tresh}(\phi(x), T) \quad \phi(x) = \sum_{i=1}^n w_i x_i \quad \phi(x_0) = T - \Delta$$

$$\phi(x_0 + z) = \sum w_i x_{0,i} + \sum w_i z_i$$

Assume an *mse*-bounded perturbation

$$\frac{\sum z_i^2}{n} \leq \gamma^2$$

\* I. Goodfellow, J. Shlens, C. Szegedy "Explaining and harnessing adversarial examples" *arXiv preprint arXiv:1412.6572* (2014).

# The linear explanation

Random perturbation

$$z_i = \gamma \cdot \mathcal{N}(0, 1)$$

$$E[\phi(x_0 + z)] = E\left[\sum_i w_i x_{0,i}\right] + E\left[\sum_i w_i z_i\right] = \phi(x_0)$$

$$\text{var}[\phi(x_0 + z)] = \text{var}\left[\sum_i w_i z_i\right] = \gamma^2 \|w\|^2$$

For the attack to succeed with non-negligible **probability** we must have

$$\gamma > \frac{k\Delta}{\|w\|}$$

# The linear explanation

Adversarial perturbation

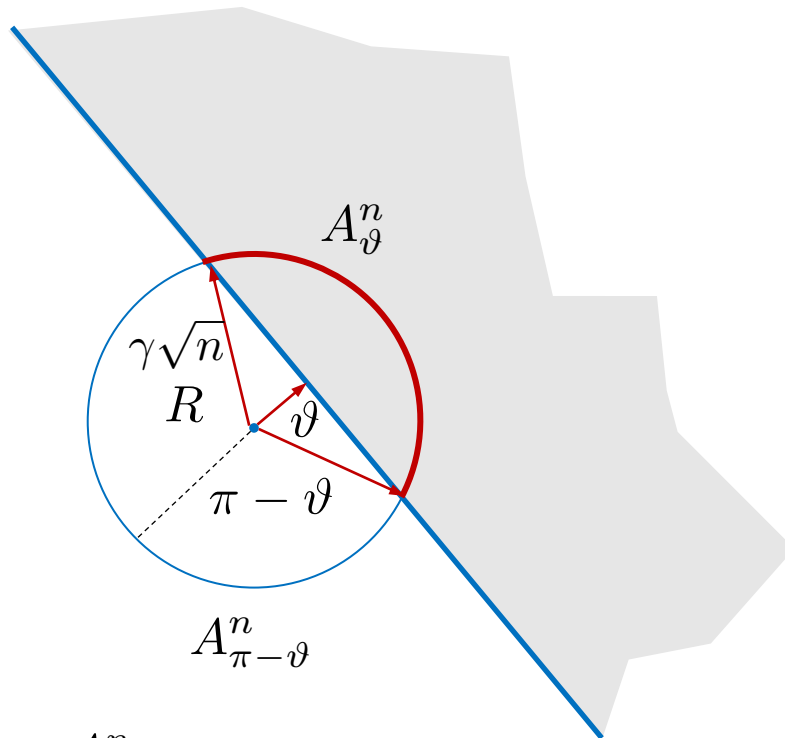
$$z = \gamma\sqrt{n} \cdot e_w$$

$$\phi(x_0 + z) = \phi(x_0) + \gamma\sqrt{n} \sum_i w_i e_{w,i} = \phi(x_0) + \gamma\sqrt{n}\|w\|$$

For the attack to succeed we must have

$$\gamma > \frac{\Delta}{\sqrt{n}\|w\|}$$

# A geometric interpretation



- In very high dimensional spaces, the *number* of directions resulting in a successful attack is very small
- This explains why adversarial examples do not show up in non-adversarial settings

$$\lim_{n \rightarrow \infty} \frac{A_{\vartheta}^n}{A_{\pi-\vartheta}^n} = 0$$

## Does it have to be linear?

- Same arguments hold if the decision function is smooth enough
- Local linearity assumption

$$\phi(x_0 + z) = \phi(x_0) + \langle \nabla \phi(x_0), z \rangle$$

- The attacker needs only to align the attack to the gradient

$$z = \gamma \sqrt{n} \cdot e_\phi$$

$$e_\phi = \frac{\nabla \phi(x_0)}{\|\nabla \phi(x_0)\|}$$

$$\gamma > \frac{\Delta}{\sqrt{n} \|\nabla \phi\|}$$



## It doesn't even need to be nearly linear

The attackability of any network can be explained by the concentration property of measure (or probability).

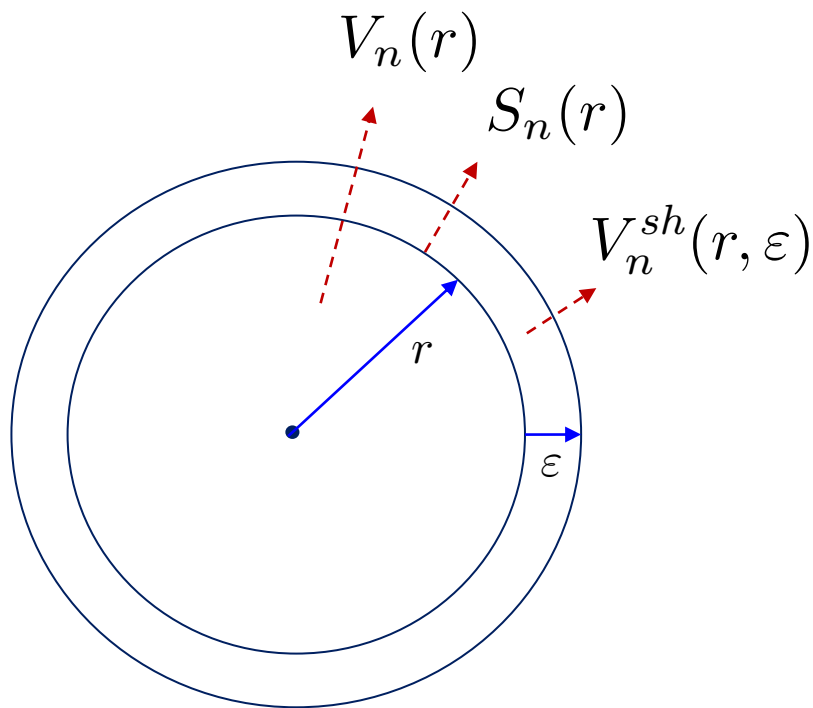
Roughly speaking it says that

*«For any measurable set in  $R^n$ , most of the volume is (arbitrarily) close to the boundary of the set»*

We'll see this for hyperspheres

# It doesn't even need to be nearly linear

Volume of a hypersphere of radius  $r$  :



$$V_n(r) = \frac{\pi^{n/2}}{\Gamma(n/2 + 1)} r^n$$

$$S_n(r) = \frac{2\pi^{n/2}}{\Gamma(n/2)} r^{n-1}$$

$$V_n(r) = \frac{r}{n} S_n(r)$$

$$V_n^{sh}(r, \epsilon) \approx S_n(r) \cdot \epsilon$$

## It doesn't even need to be nearly linear

$$\begin{aligned}\frac{V_n(r + \varepsilon)}{V_n(r)} &= \frac{V_n(r) + S_n(r)\varepsilon}{V_n(r)} \\ &= 1 + \frac{\frac{n\varepsilon}{r}V_n(r)}{V_n(r)} \\ &= 1 + \frac{n\varepsilon}{r} \\ &= \infty \text{ when } n \rightarrow \infty\end{aligned}$$

Most of the points are within  $\varepsilon$  of the boundary

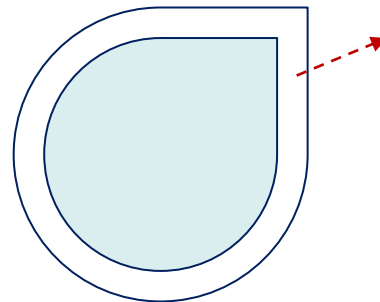
# It doesn't even need to be nearly linear

For an *mse*-bounded perturbation we have:

$$\frac{\|\varepsilon\|^2}{n} \leq \gamma^2 \implies \|\varepsilon\| \leq \sqrt{n} \gamma$$

Not only most points are within  $\varepsilon$  of the boundary,  $\varepsilon$  also increases with  $n$

By the isoperimetric inequality the above argument can be extended to any smooth enough set



Most of the volume is within  $\varepsilon$  of the boundary

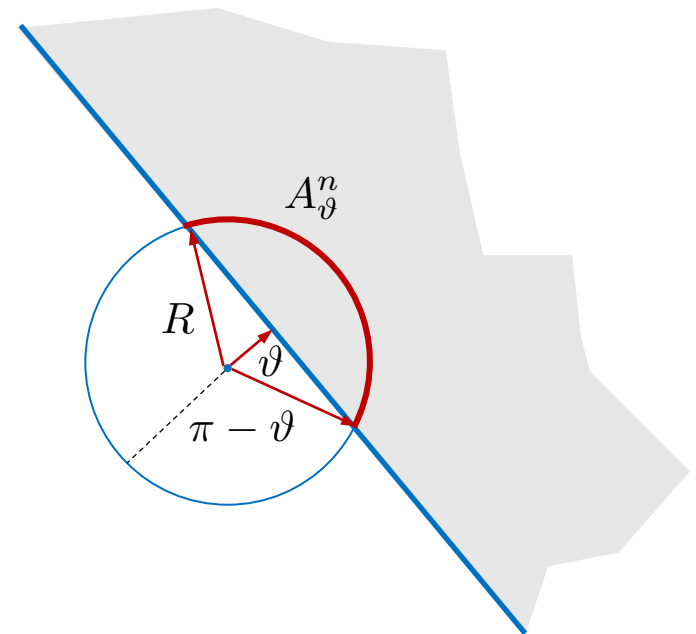
# Within a hypercube

- Most of the points within a hypersphere can be moved outside with minimal effort, **the inverse is not true due to the unboundedness of  $\mathbb{R}^n$**
- Images live in a bounded space  $\rightarrow$  the  $[0,1]^n$  hypercube
- For any 2-set partition of the hypercube (big  $n$ ) with a non-negligible volume assigned to both sets, it is always possible to move a point from one set to the other with minimal effort (bounded mse) [1]
- A binary classifier is nothing but a way to partition the hypercube
- **Do adversarial examples exist for ALL BINARY CLASSIFIERS (including the human brain)?**

[1] A. Shafahi, W. R. Huang, C. Studer, S. Feizi, T. Goldstein, «Are adversarial examples inevitable?», In International Conference on Learning Representations (2018).

# Then, what's special with DL?

- Existence of adversarial examples **does not mean they are easy to find**
- **For smooth decision functions you need to align the attack to the direction of the gradient**
- **Backpropagation provides an efficient way to compute the gradient ... then**
- **DL architectures are extremely susceptible to gradient-based attacks**

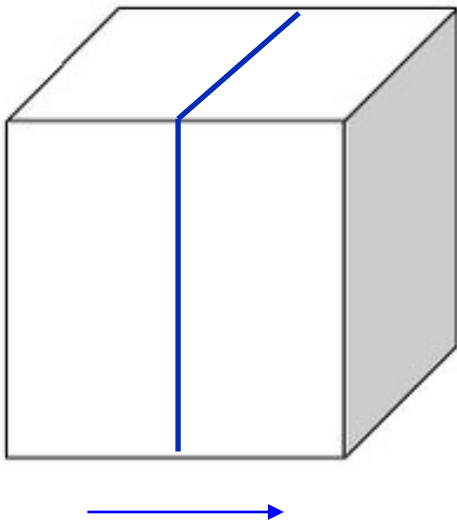


# Should we panic? Not necessarily

- Further theoretical investigation needed
- **Turning adversarial examples into real-life threats is not an easy task**
- Three major difficulties
  - Robustness
  - Lack of knowledge
  - Physical domain attacks

# Theoretical difficulties (1): infinity norm

- The theory does not generalize well to infinity norm



If the partition is aligned to one (few) dimension only, the perturbation collapses into one dimension and infinity-norm bounded adversarial perturbations may not exist

Curse of dimensionality does not apply

Should classifiers focus on few image pixels? Very likely they won't



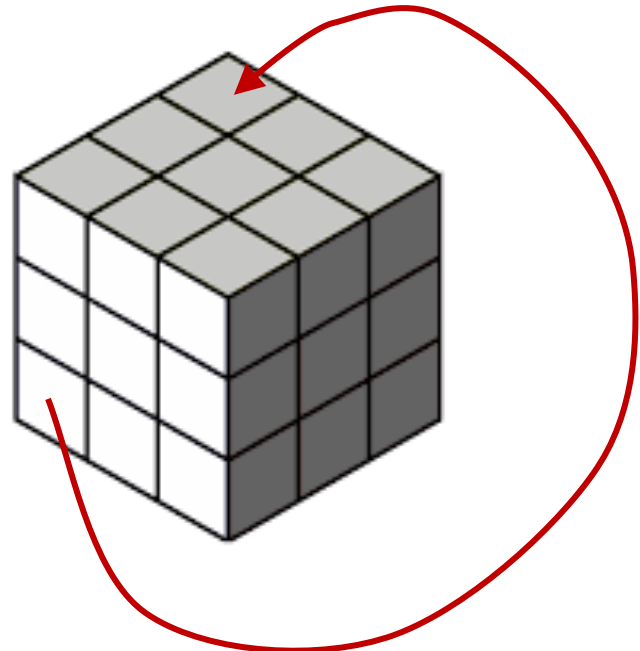
## Theoretical difficulties (2): targeted attacks

- Turning an arbitrary source class into an arbitrary target class may not always be possible
- What about multilabel classifiers?

Children playing  
football on the grass

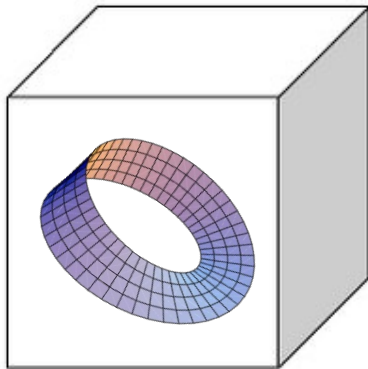


Young people drinking  
beer on a beach



### (3) Natural images do not *live* in hypercubes

- Image distribution is not uniform in hypercube
  - try generating an image at random with iid pixels uniformly distributed in  $[0,1]$  !!!



- Images likely live in thin neighborhoods of low dimensional manifolds
- Does theory generalize to manifolds? Is the size (and topology) of image manifolds large enough to trigger the large-dimensionality effects?

### (3) Natural images do not *live* in hypercubes

- Image distribution is not uniform in hypercube
  - try generating an image at random with iid pixels uniformly distributed in  $[0,1]$  !!!

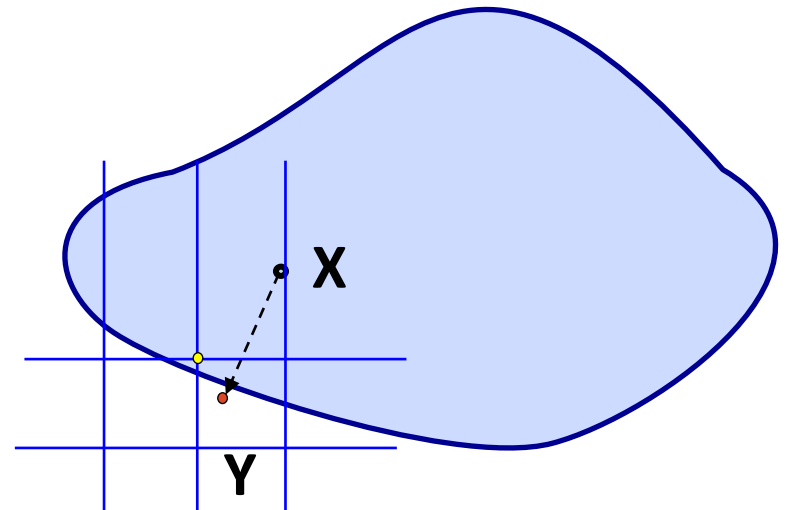
**It is a fact, that all defences proposed so far have been defeated with a limited effort ...**

- Does theory generalize to manifolds? Is the size (and topology) of image manifolds large enough to trigger the large-dimensionality effects?

# Robustness against postprocessing

- Attacks should resist to post-processing, like integer quantization or JPEG compression
- Attacked images are sometimes classified correctly after (moderate) JPEG compression\*

\* N. Das, et al. "Shield: Fast, practical defense and vaccination for deep learning using JPEG compression" Proc. 24th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining, pp. 196-204. ACM, 2018.



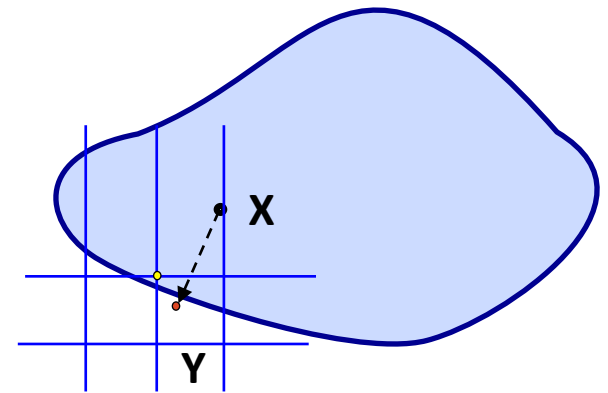
# The case of quantization

- Often attacks implemented in Foolbox result in extremely high PSNR (e.g., 60dBs)
- After quantization to integers the attack disappears

$$10 \log_{10} \frac{255^2}{MSE} = 60 \implies MSE \approx 0.06$$

- Perturbation in the order to 0.25, hence removed by integer quantization
- Specific attacks needed\*

\* Tondi, B. (2018). Pixel-domain adversarial examples against CNN-based manipulation detectors. *Electronics Letters*, 54(21), 1220-1222.



# The battle of knowledge



*If you know the enemy and know yourself, you need not fear the result of a hundred battles*



*If you know the enemy and know yourself, you need not fear the result of a hundred battles*



# Limited knowledge attacks

- The most common approach consists in attacking a **surrogate detector** (attack transferability)

$$\hat{\phi} = \hat{\phi}(\hat{\mathcal{L}}, \hat{\mathcal{W}}; \hat{\mathcal{D}})$$

- To account for mismatch in training data and architecture a stronger attack must be applied

Examples:

- N. Papernot, P. McDaniel, I. Goodfellow. "Transferability in machine learning: from phenomena to black-box attacks using adversarial samples." arXiv preprint arXiv:1605.07277 (2016).

# Attacks with limited knowledge (LK)

Attack transferability is not always easy to achieve. For instance, it turns out to be particularly difficult in MMF applications\*

\* Barni, M., Kallas, K., Nowroozi, E., & Tondi, B. (2019). On the transferability of adversarial examples against CNN-based image forensics. *IEEE Int. Conference on Acoustics, Speech and Signal Processing (ICASSP)*

## Example of *Cross-model* transferability

CROSS MODEL								
SN	TN	Accuracy w/o attack	attack	avg. PSNR	avg. L1 dist	avg. max. dist	attack success rate on SN	attack success rate on TN
$N_{BS}^R(\text{res})$	$N_{GC}^R(\text{res})$	SN= 97.60%, TN= 98.20%	I-FGSM, $\epsilon_s = 0.01$	40.02	2.53	2.55	1.0000	0.0020
$N_{BS}^R(\text{res})$	$N_{GC}^R(\text{res})$	SN= 97.60%, TN= 98.20%	I-FGSM, $\epsilon_s = 0.001$	58.48	0.31	0.33	1.0000	0.0020
$N_{BS}^R(\text{res})$	$N_{GC}^R(\text{res})$	SN= 97.60%, TN= 98.20%	JSMA, $\theta = 0.1$	46.09	0.07	57.88	1.0000	0.0164
$N_{BS}^R(\text{res})$	$N_{GC}^R(\text{res})$	SN= 97.60%, TN= 98.20%	JSMA, $\theta = 0.01$	54.98	0.04	15.14	0.9918	0.0061
$N_{BS}^R(\text{med})$	$N_{GC}^R(\text{med})$	SN= 98.20%, TN= 100%	I-FGSM, $\epsilon_s = 0.01$	40.03	2.53	2.55	<b>1.0000</b>	<b>0.8248</b>
$N_{BS}^R(\text{med})$	$N_{GC}^R(\text{med})$	SN= 98.20%, TN= 100%	I-FGSM, $\epsilon_s = 0.001$	59.67	0.26	0.27	1.0000	0.1813
$N_{BS}^R(\text{med})$	$N_{GC}^R(\text{med})$	SN= 98.20%, TN= 100%	JSMA, $\theta = 0.1$	49.64	0.03	38.11	1.0000	0.0102
$N_{BS}^R(\text{med})$	$N_{GC}^R(\text{med})$	SN= 98.20%, TN= 100%	JSMA, $\theta = 0.01$	58.47	0.02	14.05	0.9837	0.0163

Res: resizing detection

Med: median filtering  
detection

BS: Bayar-Stamm CNN with  
preprocessing

GC: Barni's net without  
preprocessing

R: Training on Raise2K

V: TraiXning on Vision dataset



# How to improve transferability

- Input diversity [1]
- Increased confidence [2]
- Distortion increases and transferability is not always easy to achieve
- Mismatch between the target system and the surrogate detector may be significant

[1] Xie C., Zhang Z., Zhou Y., Bai S., Wang J., Ren Z., Yuille A.L.: Improving transferability of adversarial examples with input diversity. CVPR, 2019.

[2] Li, W., Tondi, B., Ni, R., & Barni, M. "Increased-Confidence Adversarial Examples for Deep Learning Counter-Forensics." *Int. Conference on Pattern Recognition*. Springer, Cham, 2021.

# Attacks in the real world

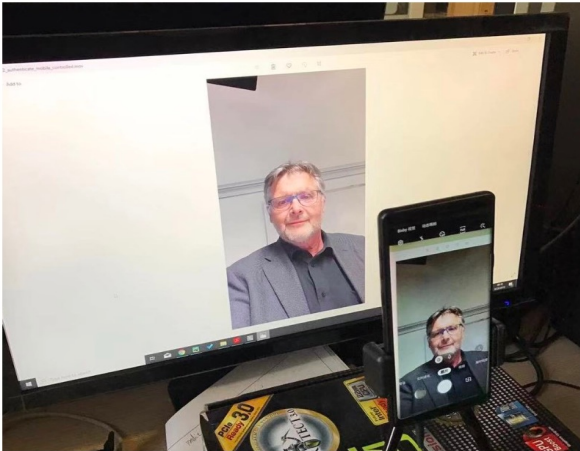
- Carrying out the attack in the physical domain is even more challenging, but still possible



- Expectation over transformation (EOT)

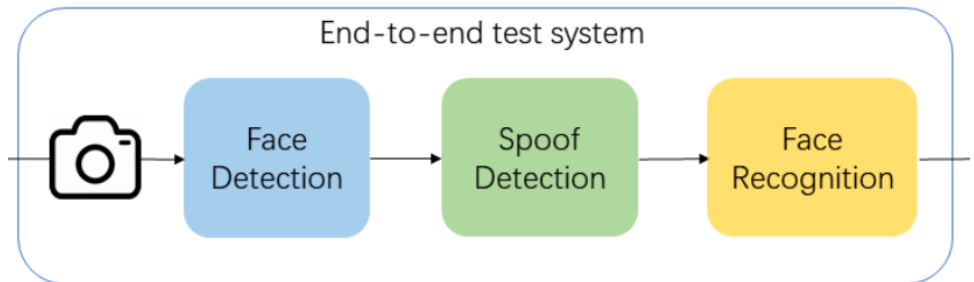
$$\rho^* = \arg \min_{\rho} E_T[\Phi(T(I + \rho))]$$

# A difficult case: attack a spoofing detector

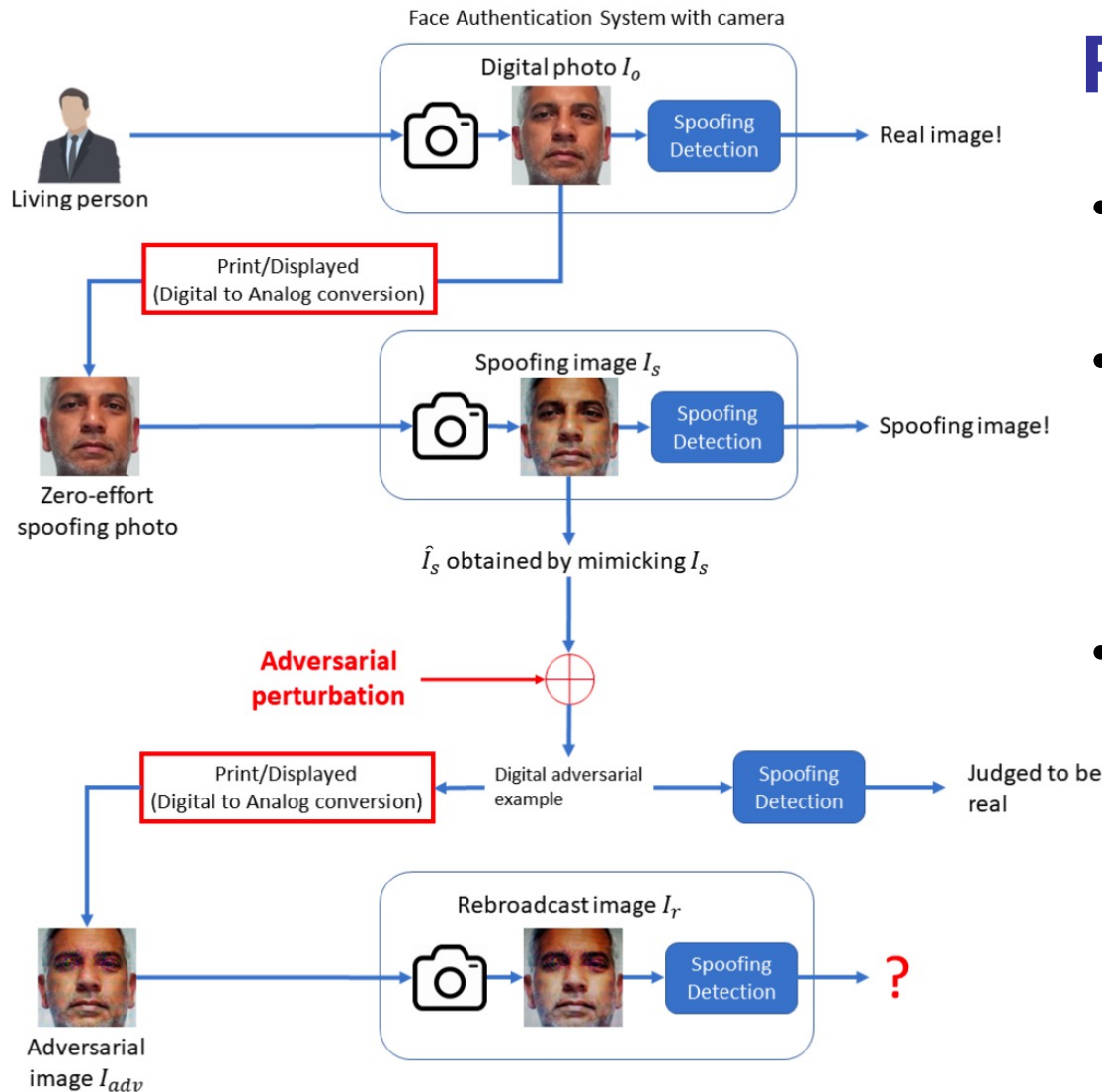


The attack must be carried out in the physical domain  
Compensate for acquisition distortions

End-to-end attack necessary



\* Zhang, B., Tondi, B., & Barni, M. (2020). Adversarial examples for replay attacks against CNN-based face recognition with anti-spoofing capability. *Computer Vision and Image Understanding*, 197, 102988.



# Pre-emptive attack

- Must mimic the acquisition pipeline
- The adversarial perturbation must survive DA and AD conversion
- The adversarial attack must work in pre-emptive way so to avoid that rebroadcasting nullifies the effect of the attack

# Attack against a spoofing detector

It ensures that the attack succeeds

It ensures that the distortion is limited

$$\min_{\rho} \mathbb{E}_{r \sim \mathcal{R}}[\mathcal{J}(f_s(r(\hat{I}_s + \rho)), l_t)] + \lambda \|\rho\|_p$$

$$s.t. \phi(f_d(r(\hat{I}_s + \rho))) = 1, \phi(f_r(r(\hat{I}_s + \rho))) = p_{\hat{I}_s}$$

It ensures that the face detector still works

It ensures that the face is recognized as the victim of the attack

$\mathcal{R}$  models the geometric and radiometric distortions introduced by the rebroadcast and re-acquisition process

# Attack against a spoofing detector

Trasformation		Range
Affine	Rotation	$[-5^\circ, 5^\circ]$
	Shear	$[-5^\circ, 5^\circ]$
	Scaling	$[0.85, 1.15]$
	Translation	$[0, 15\%]$ of image size
Perspective		$[0, 0.025]$
Brightness		$[0.85, 1.15]$
Constrast		$[0.9, 1.1]$
Gaussian Blurring(stdev)		$[0, 1]$
Hue and Saturation (value added to H and S Channel)		$[-15, 15]$

Geometric and radiometric transformations used

# Results

	PSNR	$ASR_D$ in digital domain	$ASR_P$ in physical domain
BIM	25.46	100%	21.99%
FGSM	25.59	79.86%	11.00%
GA	26.11	73.61%	15.14%
IGSA	25.32	100%	14.24%
IGA	25.34	100%	20.34%

## Attack success rate for baseline attacks

Adversarial examples	Average PSNR	$ASR_D$ in digital domain	$ASR_P$ in physical domain
Set#1	21.97	100%	79.74%
Set#2	25.08	100%	73.16%

## Attack success rate for proposed system

Attack success rate jumps to about 95% if the attacker can query the system 3 times

## Original rebroadcast



## After attack

## In summary

- The ubiquitous existence of adversarial examples raises security concerns
- Devising defenses under strong threat models (like in a white box setting) is extremely difficult

YET

- The situation may not be as bad as one could think
- Attackers have their own problems to turn adversarial examples into real world threats



## Looking ahead

- Let us focus on the **intriguing** properties of DNNs
- Unexpected observations and anomalous behaviors are a richness
- May help understanding
  - The way DNNs work
  - The space where natural images live
  - The way our brain works
- **There's a lot of exciting research in front of us**



**Thank you  
for your attention**

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